

IDENTIFYING HEALTH INSURANCE CLAIM FRAUDS USING MIXTURE OF CLINICAL CONCEPTS

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ABSTRACT

Patients depend on health insurance provided by the government systems, private systems, or both to utilize the high-priced healthcare expenses. This dependency on health insurance draws some healthcare service providers to commit insurance frauds. Although the number of such service providers is small, it is reported that the insurance providers lose billions of dollars every year due to frauds. In this paper, we formulate the fraud detection problem over a minimal, definitive claim data consisting of medical diagnosis and procedure codes. We present a solution to the fraudulent claim detection problem using a novel representation learning approach, which translates diagnosis and procedure codes into Mixtures of Clinical Codes (MCC). We also investigate

extensions of MCC using Long Short Term Memorynetworks and Robust Principal Component Analysis. Our experimental results demonstrate promising outcomes in identifying fraudulent records.

INTRODUCTION

DATA analytics has progressively become crucial to almost any economic development area. Since healthcare is one of the largest financial sectors in the US economy, the massive amount of data, including health records, clinical data, prescriptions, insurance claims, provider information, and patient information "potentially" presents incredible opportunities for data analysts. Health insurance agencies process billions of claims every year and healthcare expenses is over three trillion dollars in the United States [1]. Figure 1 presents a concise flow of a typical care

ISSN 2454-5007, www.ijmm.net Vol. 15, Issue. 1, March 2023 n or some other entities" [3]. Those ricated claims bear a very high cost

the patient has adequate coverage through his/her insurance plan or other funds before getting any service. Next, the service provider identifies relevant based on the diagnoses initial examinations performed on the patient. The service provider then runs tests on the patient using one or more medical interventions such as further diagnostics and surgical procedures. These diagnoses and procedures are usually tagged with the patient's report along with other information such as personal, demographic, and past/present visit information. At this point, the patient typically pays a copay defined in his/her insurance plan and checks out. Then, the patient's report is sent to a medical coder who abstracts the information and creates a "superbill" containing all information about the provider, Given the economic volume of the healthcare industry, it is natural to observe fraudulent and fabricated claims submitted to insurance companies. The National Health Care Anti- Fraud Association (NHCAA) defines healthcare fraud "An as intentional deception or misrepresentation made by a person, or an entity, with the knowledge that the deception could result in some unauthorized benefit to

him or some other entities" [3]. Those fabricated claims bear a very high cost, albeit they constitute a small fraction. According to NHCAA

the fraud related financial loss is in the orders of tens of billions of dollars in the United States [3]. Although there are strict policies regarding fraud and abuse control in healthcare industries, studies show that a very small portion of the losses

are recovered annually [4].

Most typical fraudulent activities committed by dishonest providers in the healthcare domain include the following.

_ Making false diagnoses to justify procedures that are not medically necessary.

_ Billing for high priced procedures or services instead of the actual procedures, also called "upcoding".

_ Fabricating claims for unperformed procedures.

_ Performing medically unnecessary procedures to claim insurance payments.

_ Billing for each step of a procedure as if it is a separate procedure, also called "unbundling".

_ Misrepresenting non-covered treatments as medically necessary to

receive insurance payments, especially for cosmetic procedures.

It is not feasible or practical to apply only domain knowledge to solve all or a subset of the issues listed above. Automated data analytics can be employed to detect fraudulent claims at an early stage and immensely help domain experts to manage the fraudulent activities much better.

In this paper, we focus on the problem of healthcare fraud detection from health insurance providers' viewpoint. We answer the question of how to classify a procedure as legitimate or fraudulent from a claim when we only have limited data available, i.e. diagnosis and procedure codes. The problem of fraud detection in medical domain has been identified using different approaches such as data mining [5], classification methods [6], [7], Bayesian analysis [8], statistical surveys [9], nonparametric approaches [10], and expert analysis. Existing methods use physicians profile, background history, claim amount, service quality, services performed per provider, and related metrics from a claim database to create models for claim status prediction. Although these methods are successful, they often employ datasets that are not

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publicly available. Furthermore, the variables featured in those datasets are diverse and generally incompatible, which makes the solutions very difficult to transfer. In this study we limit our available data to diagnosis and procedure codes, because obtaining third-party access to richer datasets is often Insurance prohibited by Health Portability and Accountability Act (HIPAA) in the US, General Data Protection Regulation (GDPR) in Europe or similar law in other regions. Besides, the healthcare industry is more apprehensive to share data compared to other sectors. Moreover, different software systems report different patient variables, which prohibits transferring solutions from one system to another. As a result, we confine our problem formulation to diagnosis and procedure codes which can always be handled in the same way whether they are countryspecific or international. Our solution approach assumes the claim data as a mixture of medical concepts with respect to clinical codes of diagnoses and procedures in International Classification of Diseases (ICD) coding format. Moreover, the proposed approach works on other coding formats, e.g., Current Procedural

Terminology (CPT) and Healthcare Common Procedure Coding System (HCPCS), or their combinations without any modification.

We represent an insurance claim as a Mixture of latent Clinical Concepts using probabilistic (MCC) topic modeling. To the best of our knowledge this is the first work representing insurance claims as mixtures of clinical concepts in a latent space. We assume that every claim is a representation of latent or obvious mixtures of clinical concepts such as pain, mental or infectious diseases. Moreover, each clinical concept is a mixture of clinical codes, i.e., diagnosis and procedure codes. The intuition behind our model comes from the services provided by doctor's offices, clinics, and hospitals. In general, a patient gets services based on specific issues consisting of one or more diagnoses. Next, the service provider performs necessary procedures to treat the patient. Therefore, the diagnoses and procedures in a claim can be represented as a mixture of clinical concepts such as pain, mental, infectious diseases and/or their treatments. Note that, we do not explicitly label or interpret these concepts, as they are

often not obvious, complex or require domain knowledge.

We extend the MCC model using Long-Short Term Memory networks and Robust Principal Component Analysis. Our goal in extending MCC is to filter the significant concepts from claims and classify them as fraudulent or nonfraudulent. We extend MCC by using the concept weights of a claim as a sequence representation within a Long- Short Term Memory (LSTM) network. This network allows us to represent the claims as sequences of dependent concepts to be classified by the LSTM. Similarly, we apply Robust Principal Component Analysis (RPCA) to filter significant concept weights by decomposing claims into a low-rank and sparse vector representations. The low- rank matrix ideally captures the noise- free weights.

Our unique contributions in this study can be summarized

as follows.

We formulate the fraudulent claim detection problem over a minimal, definitive claim data consisting of procedure and diagnosis codes.

_ We introduce clinical concepts over procedure and diagnosis codes as a new representation learning approach.

_ We extend the mixtures of clinical concepts using LSTM and RPCA for classification.

We compare our approaches to the Multivariate Outlier Detection (MOD) [11] and a baseline method and report improved performance. Multivariate Outlier Detection method consists of two steps which are used to detect anomalous provider payments within Medicare claims data. In the first step, a multivariate regression model is built on 13 hand picked features to generate corresponding residuals. Next, the residuals are used as inputs to a generalized univariate probability model. Specifically, they used probabilistic programming methods in Stan [12] to identify possible outliers in the claim data. The authors use the same CMS (Centers for Medicare and Medicaid Services) dataset that we use in our experiments with a different problem formulation. Their study incorporates providers and beneficiary data that was related to Medicare beneficiaries within the state of Florida, while we employ MOD on MCC features. On the other hand, the baseline

classifier assigns a test claim as the majority label present in the training claim data.

Our experimental results show that MCC + LSTM reaches an accuracy, precision, and recall scores of 59%, 61%, and 50%, respectively on the inpatient dataset obtained from CMS. In addition, it demonstrates 78%, 83%, and 72% accuracy, precision, and recall scores, respectively on the outpatient dataset We believe that the proposed problem formulation, representation learning and solution will initiate new research on claim detection fraudulent using minimal, but definitive data. The rest of the paper is organized as follows.

EXISTING SYSTEM

Yang and Hwang developed a fraud detection model using the clinical pathways concept and process-mining framework that can detect frauds in the healthcare domain [13]. The method uses a module that works by discovering structural patterns from input positive and negative clinical instances. The most frequent patterns are extracted from every clinical instance using the module. Next, a feature-selection module is used to create a filtered dataset with labeled features. Finally, an inductive model is built on the feature set for evaluating new claims. Their method uses clustering, association analysis, and principal component analysis. The technique was applied on a real-world data set collected from National Health Insurance (NHI) program in Taiwan. Although the authors constructed different features to generate patterns for both normal and abusive claims, the significance of those features is not discussed.

Bayerstadler et al. [14] presented a predictive model to detect fraud and abuse using manually labeled claims as training data. The method is designed to predict the fraud and abuse score using a probability distribution for new claim invoices. Specifically, the authors Bayesian network proposed a to summarize medical claims' representation patterns using latent variables. In the prediction step, a multinomial variable modeling predicts the probability scores for various fraud events. Additionally, they estimated the model parameters using Markov Chain Monte Carlo (MCMC) [15].

Zhang et al. [16] proposed a Medicare fraud detection framework using the concept of anomaly detection [17]. First ISSN 2454-5007, www.ijmm.net Vol. 15, Issue. 1, March 2023

part of the proposed method consists of a spatial density based algorithm which is claimed to be more suitable compared to local outlier factors in medical insurance data. The second part of the method uses regression analysis to identify the linear dependencies among different variables. Additionally, the authors mentioned that the method has limited application on new incoming data.

Kose et al. [18] used interactive unsupervised machine learning where expert knowledge is used as an input to the system to identify fraud and abuse related legal cases in healthcare. The authors used a pairwise comparison method of analytic hierarchical process (AHP) to incorporate weights between (patients) and attributes. actors Expectation maximization (EM) is used to cluster similar actors. They had domain experts involved at different levels of the study and produced storyboard based abnormal behavior traits. The proposed framework is evaluated based on the behavior traits found using the storyboard and later used for prescriptions by including all related persons and commodities such as drugs.

Fabricating claims for unperformed procedures.

Performing medically unnecessary procedures to claiminsurance payments. Billing for each step of a procedure as if it is a separateprocedure, also called "unbundling".

Misrepresenting non-covered treatments as medicallynecessary to receive insurance payments, especially forcosmetic procedures.

PROPOSED SYSTEM

We extend the MCC model using Long-Short Term Memory networks and Robust Principal Component Analysis. Our goal in extending MCC is to filter the significant concepts from claims and classify them as fraudulent or nonfraudulent. We extend MCC by using the concept weights of a claim as a sequence representation within a Long-Short Term Memory (LSTM) network. This network allows us to represent the claims as sequences of dependent concepts to be classified by the LSTM. Similarly, we apply Robust Principal Component Analysis (RPCA) to filter significant weights concept by decomposing claims into a low-rank and sparse vector representations. The lowrank matrix ideally captures the noisefree weights.

Bauder and Khoshgoftaar [19] proposed a general outlier detection model using Bayesian inference to screen healthcare claims. They used Stan model which is similar to [20] in their experiments. Note that, they consider only provider levelfraud detection without considering clinical code based relations. Many of those methods use private datasets or different datasets with incompatible feature lists. Therefore, it is very difficult to directly compare these studies. In addition, HIPAA, GDPR and similar law enforce serious penalties for violations of the privacy and security of healthcare information, which make healthcare providers and insurance companies very reluctant to share rich datasets if not at all. For these reasons, we formulate the problem over a minimal, definitive claim data consisting of diagnosis and procedure codes. Under this setting we tackle the problem of flagging a procedure as legitimate or fraudulent using mixtures of clinical codes along with RNN and RPCA based encodings.

Disadvantages

Making false diagnoses to justify procedures that are not medically necessary.

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Our unique contributions in this study can be summarized as follows.

The system formulates the fraudulent claim detection problem over a minimal, definitive claim data consisting of procedure and diagnosis codes.

The system introduces clinical concepts over procedure and diagnosis codes as a new representation learning approach.

The system extends the mixtures of clinical concepts using LSTM and RPCA for classification.

Advantages

The proposed system uses Support Vector Machine (SVM) for classification with MCC.

➢ Multivariate Outlier Detection method is an effective method which is used to detect anomalous provider payments within Medicare claims data.

IMPLEMENTATION

Service Provider

In this module, the Service Provider has to login by using valid user name and password. After login successful he can do some operations such as

Login, Browse and Train & Test Health Insurance Data Sets, View Trained and Tested Accuracy in Bar Chart, View Trained and Tested Accuracy Results, View Prediction Of Health Insurance Fraud Type, View Health Insurance Fraud Type Ratio, Download Predicted Data Sets, View Health Insurance Fraud Type Ratio Results, View All Remote Users

View and Authorize Users

In this module, the admin can view the list of users who all registered. In this, the admin can view the user's details such as, user name, email, address and admin authorizes the users.

Remote User

In this module, there are n numbers of users are present. User should register before doing any operations. Once user registers, their details will be stored to the database. After registration successful, he has to login by using authorized user name and password. Once Login is successful user will do some operations like REGISTER AND LOGIN. PREDICT HEALTH INSURANCE CLAIM FRAUD TYPE, VIEW YOUR PROFILE.





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Fig.2. Register page.



Fig.3. User details.

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Fig.4. Login details.

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Fig.5. Dataset details.



Fig.6. Output results.

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Fig.7. Output results. CONCLUSION

In this paper, we pose the problem of fraudulent insurance claim identification as a feature generation and classification process. We formulate the problem over definitive claim minimal. data a consisting of procedure and diagnosis codes, because accessing richer datasets are often prohibited by law and present inconsistencies among different software systems. We introduce clinical concepts over procedure and diagnosis codes as a new representation learning approach. We assume that every claim is a representation of latent or obvious Mixtures of Clinical Concepts which in

turn are mixtures of diagnosis and procedure codes. We extend the MCC model using Long-Short Term Memory network (MCC + LSTM) and Robust Principal Component Analysis (MCC + RPCA) to filter the significant

concepts from claims and classify them as fraudulent or non fraudulent. Our results demonstrate an improvement scope to find fraudulent healthcare claims with minimal information. Both MCC and MCC + RPCA exhibit consistent behavior for varying concept sizes and replacement probabilities in the negative claim generation process. MCC + LSTM reaches an accuracy, precision, and recall scores of 59%, 61%, and 50%, respectively on the inpatient dataset. Besides, it presents 78%, 83%, and 72% accuracy, precision, and recall scores, respectively on the outpatient dataset. We notice similarity between the results of MCC and MCC + RPCA, as both use an SVM classifier. We believe that the proposed problem formulation, representation learning and solution will initiate new research on fraudulent insurance claim detection using minimal, but definitive data.

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